5.1 Operations with Polynomials

Honors Algebra 2

|  | Expanded Form | Simplified |
| :--- | :--- | :--- |
| 1. $a^{5} \cdot a^{2}$ |  |  |
| 2. $\left(a^{5}\right)^{2}$ |  |  |
| 3. $\left(4 a^{2}\right)^{3}$ |  |  |
| 4. $\left(3 a^{2} b^{3}\right)^{4}$ | $(3 \cdot 4)^{2}=$ |  |
|  |  |  |
| $3 \cdot 4^{2}=$ | $-(3 \cdot 4)^{2}=$ |  |
| $(-3 \cdot 4)^{2}=$ |  |  |

Rules for Multiplying Monomials

| Product of Powers | $a^{m} \cdot a^{n}$ |  |
| :--- | :---: | :--- |
| Power of a Power | $\left(a^{m}\right)^{n}$ |  |
| Power of Products | $(a b)^{m}$ |  |
| Power of a Monomial | $\left(a^{m} b^{n}\right)^{p}$ |  |

Examples-Simplify the following:

| 5. $\left(\frac{1}{2} a^{2} b\right)^{3}$ | 6. $\left(2 a^{4}\right)\left(3 a^{3} b\right)\left(-4 a^{2} b^{3}\right)^{2}$ |
| :--- | :--- | :--- |
| 7. $9\left(\frac{1}{3} a^{3} b^{4}\right)^{2}$ | $8 .\left(-4 x^{5}\right)^{3}$ |
| 9. $\left(-5 a^{3}\right)^{2}+(3 a)^{3}$ | $10 .\left(5 a^{3}\right)^{2}+\left(2 a^{2}\right)^{3}$ |

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| :--- | :--- | :--- | :--- |
| 11. $\frac{a^{5}}{a^{3}}$ |  |  |  |
| 12. $\frac{a^{3}}{a^{5}}$ |  |  |  |
| 13. $\frac{4 a^{2} b^{3}}{8 a b^{5}}$ |  |  |  |
| 14. $\frac{a^{4}}{a^{4}}$ |  |  |  |


| Rules for Dividing Monomials |  |  |
| :--- | :---: | :--- |
| Quotient of Powers | $\frac{a^{m}}{a^{n}}$ |  |
| Zero Exponent | $a^{0}$ |  |
| Negative Exponent | $a^{-1}$ |  |

Examples- Simplify the following:

| 15. $\frac{144 x^{5} y^{-3} z^{4}}{12 x^{6} y^{2} z^{4}}$ | 16. $\frac{\left(3 x^{5}\right)^{2}}{\left(-2 x^{3}\right)^{-3}}$ |
| :--- | :--- |
| 17. $\frac{x^{5} y^{2}}{x y^{3}}$ | $18 . \quad\left(\frac{2 a^{3}}{b^{-4}}\right)^{-2}$ |
| 19. $\frac{\left(x^{4} y^{-7}\right)^{0}}{(-3)^{2}}$ | 20. $\frac{1}{x^{0}+y^{0}}$ |

Degree of a Polynomial: the degree of the monomial with the greatest degree.

What is the degree of:

| $f(x)=6 x^{7}+9 x^{2}+3 x^{10}$ | $f(x)=x^{2}+2 x^{3}-x$ |
| :--- | :--- |

Simplify:

1. $\left(4 x^{3}+4 x^{2}-3 x\right)+\left(-5 x^{3}-2 x^{2}-4\right) \quad$ 2. $\left(-4 x^{3}+6 x^{2}-3\right)-\left(3 x^{4}+4 x^{2}+7 x+12\right)$

Multiplying Polynomials: Distribute, combine like terms, and write in descending order.
3. $(x-5)\left(x^{2}-2 x+3\right)$
4. $\left(2 x^{3}+5 x^{2}-6 x+1\right)(3 x-2)$

