

Student Objectives:

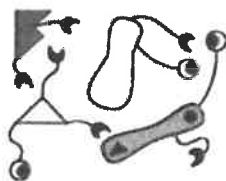
- The student will be able to write a working definition for types of angles.
- The student will be able to use counterexamples to refine definitions.
- The student will be able to recall and apply special angle relationships.

Good Definitions are Important!

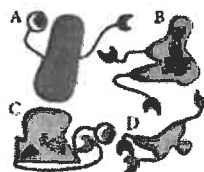
1. Take a look at the picture below. Which are widgets in the last grouping below?



Widgets



Not Widgets



Which are Widgets?

A
widget
|
one eye, one arm
colored body

2. Everyone knows that a "square is figure with four equal sides." What is wrong with this definition?

counterexample : an example that disproves a statement

counterexamples:

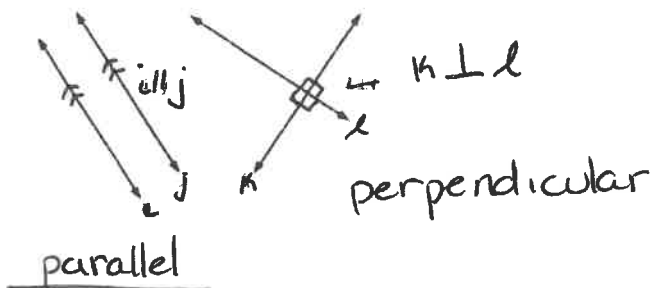


square : a 4-sided figure that has all sides congruent and all angles measuring 90°

Definition:

- 1) Classify your term (what is it?)
- 2) Differentiate your term (what is special about it?)
- 3) Test your definition by looking for counterexamples

More Markings:



Define:

Parallel Lines are lines in the same plane that never meet

classify

differentiate

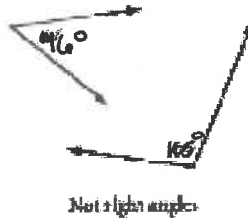
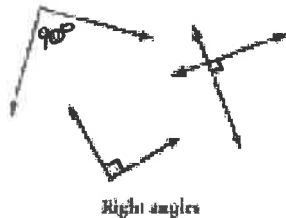
Perpendicular Lines are lines that meet at 90°

classify

differentiate

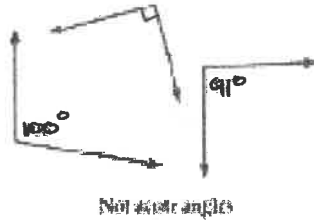
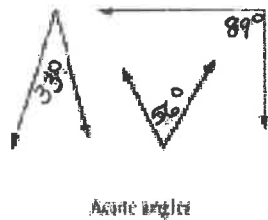
3. Here are some examples and non-examples of special types of angles.
 - a. Write a definition for each boldfaced term. Make sure your definitions highlight important differences.
 - b. Trade definitions and test each other's definitions by looking for **counterexamples**.
 - c. If another group member finds a counterexample to one of your definitions write a better definition. As a group decide on the best definition for each term.
 - d. We will discuss together as a class!

Right Angle



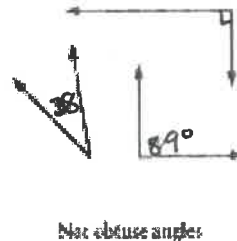
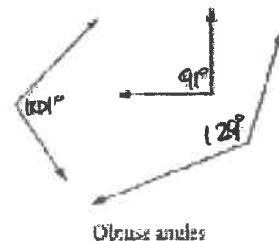
A right angle is an angle that measures 90°

Acute Angle



An acute angle is an angle that measures less than 90°

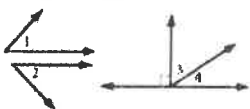
Obtuse Angle



An obtuse angle is an angle that measure greater than 90° but less than 180°

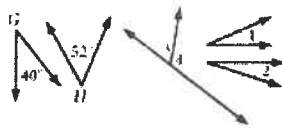
Complementary Angles

$m\angle 1 + m\angle 2 = 90^\circ$



Pairs of complementary angles:
 $\angle 1$ and $\angle 2$
 $\angle 3$ and $\angle 4$

$m\angle 1 + m\angle 2 \neq 90^\circ$



Not pairs of complementary angles:
 $\angle G$ and $\angle H$ $\angle 1$ and $\angle 2$
 $\angle 3$ and $\angle 4$

A pair of complementary angles has a sum of 90°

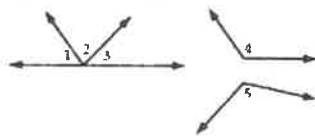
Supplementary Angles

$m\angle 3 + m\angle 4 = 180^\circ$



Pairs of supplementary angles:
 $\angle 1$ and $\angle 2$
 $\angle 3$ and $\angle 4$

$m\angle 4 + m\angle 5 > 180^\circ$



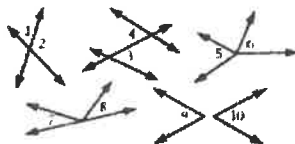
Not pairs of supplementary angles:
 $\angle 1, \angle 2,$ and $\angle 3$
 $\angle 4$ and $\angle 5$

A pair of supplementary angles has a sum of 180°

Vertical Angles



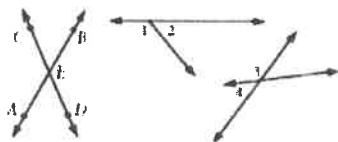
Pairs of vertical angles:
 $\angle 1$ and $\angle 2$
 $\angle 3$ and $\angle 4$
 $\angle AED$ and $\angle BEC$
 $\angle AEC$ and $\angle DEB$



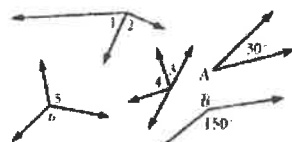
Not pairs of vertical angles:
 $\angle 1$ and $\angle 2$
 $\angle 3$ and $\angle 4$
 $\angle 5$ and $\angle 6$
 $\angle 7$ and $\angle 8$
 $\angle 9$ and $\angle 10$

Vertical angles are formed by 2 intersecting lines; they share a common vertex but no common side

Linear Pair of Angles



Linear pairs of angles:
 $\angle 1$ and $\angle 2$
 $\angle 3$ and $\angle 4$
 $\angle AED$ and $\angle AEC$
 $\angle BED$ and $\angle DEA$

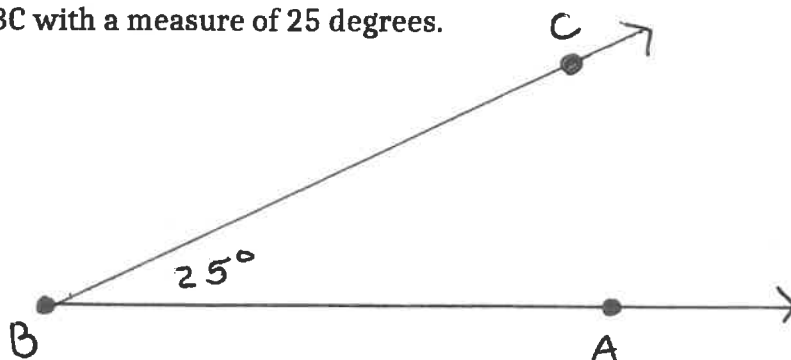


Not linear pairs of angles:
 $\angle 1$ and $\angle 2$
 $\angle 3$ and $\angle 4$
 $\angle 5$ and $\angle 6$
 $\angle A$ and $\angle B$

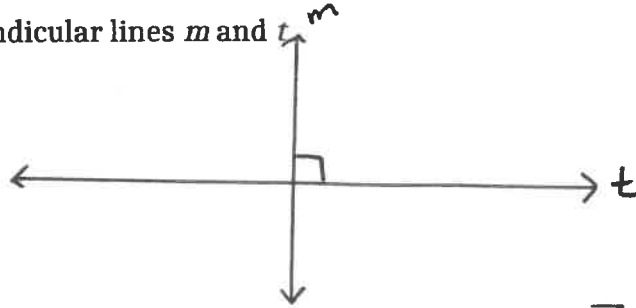
Two angles are a linear pair if they share a vertex and a common side and their noncommon sides form a line

Examples:

- Draw and carefully label the figures below. Use the appropriate marks to indicate the figures. Use a protractor and ruler.
 - Acute angle ABC with a measure of 25 degrees.



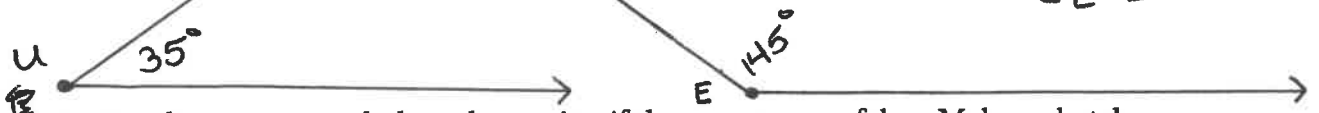
b. Perpendicular lines m and t



c. Supplementary angles $\angle U$ and $\angle E$ where $\angle U = 35^\circ$

add up to 180°

$$\begin{aligned} \angle U + \angle E &= 180^\circ \\ 35^\circ + \angle E &= 180^\circ \\ -35^\circ & \quad -35^\circ \\ \angle E &= 145^\circ \end{aligned}$$



2. For the statements below, determine if they are true or false. Make a sketch demonstrating each true statement. For each false statement, draw a counterexample.

a. For every line segment there is exactly one midpoint.

b. If $CA = AT$, then A is the midpoint of \overline{CT} .

c. If two different circles intersect, then they intersect at one and only one point.

- d. If $m\angle D = 40^\circ$ and $m\angle C = 140^\circ$, then the angles are a linear pair.

