October 2018 \#19
Given three positive integers $a, b$, and $c$, such that $a^{2}+b^{2}=c^{2}$. Prove that
$(2 a+b+2 c)^{2}+(a+2 b+2 c)^{2}=$ $(2 a+2 b+3 c)^{2}$.

April 2014 \#12
If

$$
\begin{aligned}
& f(x)=x^{2}+b x+c \\
& f(1)=9, \text { and } \\
& f(3)-f(2)=8
\end{aligned}
$$

find $f(4)$.

## September 2014 \#14

Find the sum of the solutions to the equation $3\left(3^{2 x}\right)-28\left(3^{x}\right)=-9$. (Use a calculator in the final step.)

October 2014 \#13
Solve the following system of equations:

$$
\left\{\begin{array}{l}
\frac{3}{x+1}+\frac{5}{y-2}=1 \\
\frac{6}{x+1}+\frac{1}{y-2}=5
\end{array}\right\}
$$

Math Team Oct 2017 \#3

$$
\text { If } p^{*} q=(p-q)(p+q) \text { and } p \Delta q=(p+q)^{2}-2 p q \text {, find }(3 * 4)(3 \Delta 4) \text {. }
$$

