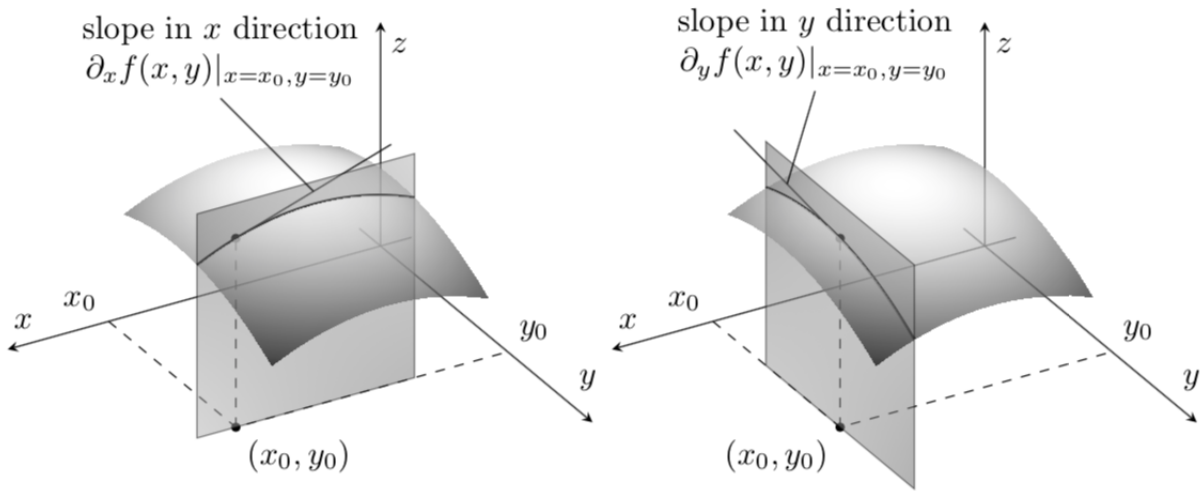


## 15.3 Partial Derivatives Multivariable Calculus

Partial derivatives are computed just like ordinary derivatives in one variable with this difference: To compute  $f_x$ , treat  $y$  as a constant, and to compute  $f_y$ , treat  $x$  as a constant.



1. Compute the partial derivatives of  $f(x, y) = x^2 y^5$

2. Calculate  $g_x(1, 3)$  and  $g_y(1, 3)$ , where  $g(x, y) = \frac{y^2}{(1+x^2)^3}$

3. Calculate  $\frac{d}{dx} \sin(x^2 y^5)$

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4. Calculate  $f_z(0, 0, 1, 1)$ , where  $f(x, y, z, w) = \frac{e^{xz+y}}{z^2+w}$

5. Calculate the second-order partial derivatives of  $f(x, y) = x^3 + y^2 e^x$

6. Calculate  $f_{xyy}$  for  $f(x, y) = x^3 + y^2 e^x$

**Clairut's Theorem: Equality of Mixed Partial**

If  $f_{xy}$  and  $f_{yx}$  are both continuous functions on a disk  $D$ , then  $f_{xy}(a, b) = f_{yx}(a, b)$  for all  $(a, b) \in D$ .

$$\frac{d^2 f}{dx dy} = \frac{d^2 f}{dy dx}$$

7. Calculate the partial derivative  $g_{zzwx}$  where  $g(x, y, z, w) = x^3 w^2 z^2 + \sin\left(\frac{xy}{z}\right)$