## Continuity:

## 4 types of Discontinuity:

1. 
2. 
3. 
4. Find the points of discontinuity in $f(x)=\frac{x^{2}-2 x-3}{x^{2}+x-12}$ and determine each type of discontinuity.

## Intermediate Value Theorem for Continuous Functions:

A function $y=f(x)$ that is continuous on a closed interval $[a, b]$ takes on every value between $f(a)$ and $f(b)$. In other words, if $y_{0}$ is between $f(a)$ and $f(b)$, then $y_{0}=f(c)$ for some $c$ in $[a, b]$.

2. Let $f(x)=x^{2}+2 x-8$. Prove that there is an $x$-intercept from $[1,3]$.
3. Find each point of discontinuity for the function below. Then if there are any, determine if the discontinuities are removable.

$$
f(x)=\left\{\begin{array}{lr}
-2 x, & \leq 2 \\
x^{2}-4 x+1, & x>2
\end{array}\right.
$$

4. Find the constant $a$, such that the function is continuous on the entire number line.

$$
f(x)=\left\{\begin{array}{cc}
x^{3}, & x \leq 2 \\
a x^{2}, & x>2
\end{array}\right.
$$

2.3 Continuity

