

The Fundamental Theorem of Calculus (FTC)	
Part 1	Part 2
<p>If f is continuous on $[a, b]$, then the function</p> $F(x) = \int_a^x f(t) dt$ <p>has a derivative at every point x in $[a, b]$, and</p> $\frac{dF}{dx} = \frac{d}{dx} \int_a^x f(t) dt = \underline{\hspace{2cm}}$	<p>If f is continuous on $[a, b]$, and if F is any antiderivative of f on $[a, b]$, then</p> $\int_a^b f(x) dx = \underline{\hspace{2cm}}$

1. Find $\frac{dy}{dx}$

a. $y = \int_2^x (3t + \cot(t^2)) dt$

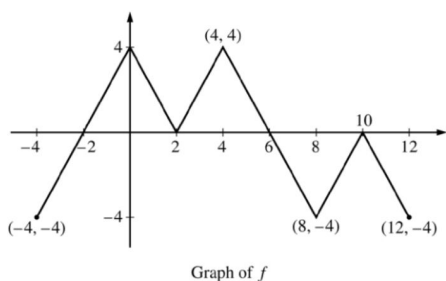
c. $y = \int_6^{x^2} \cot 3t \, dt$

b. $y = \int_4^x e^u \sec u \, du$

d. $y = \int_{3x^2}^{5x} \ln(2 + p^2) dp$

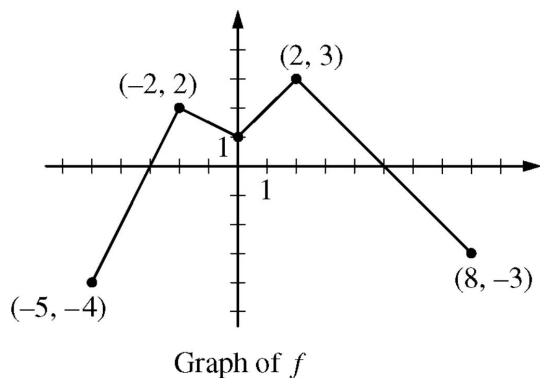
2. The figure below shows the graph of the piecewise-linear function f . For $-4 \leq x \leq 12$, the function g is defined by $g(x) = \int_{-4}^x f(t) dt$. Does g have a relative minimum, a relative maximum, or neither at $x = 10$? Justify your answer.

AB Calculus
6.4 Fundamental Theorem of Calculus



3. The functions f and g are given by $f(x) = \int_0^{3x} \sqrt{4+t^2} dt$ and $g(x) = f(\sin x)$. Find $f'(x)$ and $g'(x)$.

4. The continuous function f is defined on the interval $-5 \leq x \leq 8$. The graph of f which consists of four line segments is shown in the figure below. Let g be the function given by $g(x) = 2x + \int_{-2}^x f(t) dt$. Find $g'(x)$ in terms of $f(x)$. For each of $g''(4)$ and $g''(-2)$, find the value or state that it does not exist.



5. Evaluate each integral using the Evaluation Part of the Fundamental Theorem:

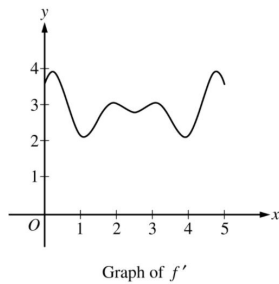
a. $\int_2^{-1} 3^x dx$

b. $\int_0^5 x^{\frac{3}{2}} dx$

d. $\int_0^4 \frac{1-\sqrt{u}}{\sqrt{u}} du$

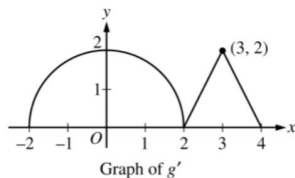
c. $\int_{\frac{\pi}{6}}^{\frac{5\pi}{6}} \csc^2 \theta d\theta$

6. The graph of f' , the derivative of f , is shown below. If $f(0) = 20$, which of the following could be the value of $f(5)$?



- (A) 15
(B) 20
(C) 25
(D) 35
(E) 40

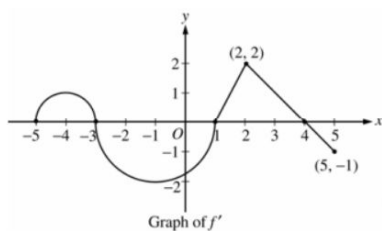
7. The graph of g' , the first derivative of g , consists of a semicircle of radius 2 and two line segments, as shown in the figure below. If $g(0) = 1$, what is $g(3)$?



- (A) $\pi + 1$
(B) $\pi + 2$
(C) $2\pi + 1$
(D) $2\pi + 2$

8. Let f be a function defined on the closed interval $-5 \leq x \leq 5$ with $f(1) = 3$. The graph of f' the derivative of f , consists of two semicircles and two line segments, as shown below. Find the absolute minimum value of $f(x)$ over the closed interval $-5 \leq x \leq 5$. Explain your reasoning.

AB Calculus
6.4 Fundamental Theorem of Calculus



9. Find the total area of the region bounded between the curve and the x-axis of $y = 3x^2 - 3$ on $-2 \leq x \leq 2$