## Ellipse:

## Major and Minor Axis:

## Constant Sum



| KeyConcept Equations of Ellipses Centered at the Origin |  |  |
| :--- | :---: | :---: |
| Standard Form | $\frac{x^{2}}{a^{2}}+\frac{y^{2}}{b^{2}}=1$ | $\frac{y^{2}}{a^{2}}+\frac{x^{2}}{b^{2}}=1$ |
| Orientation | horizontal | vertical |
| Foci | $(c, 0),(-c, 0)$ | $(0, c),(0,-c)$ |
| Length of Major Axis | $2 a$ units | $2 a$ units |
| Length of Minor Axis | $2 b$ units | $2 b$ units |

## Important Relationships:

1. Write the equation for the ellipse:

2. Write an equation for an ellipse with vertices at $(-4,0)$ and $(4,0)$ and foci at $(2,0)$ and $(-2,0)$.

KeyConcept Equations of Ellipses Centered at ( $h, \boldsymbol{k}$ )

| Standard Form | $\frac{(x-h)^{2}}{a^{2}}+\frac{(y-k)^{2}}{b^{2}}=1$ | $\frac{(y-k)^{2}}{a^{2}}+\frac{(x-h)^{2}}{b^{2}}=1$ |
| :--- | :---: | :---: |
| Orientation | horizontal | vertical |
| Foci | $(h \pm c, k)$ | $(h, k \pm c)$ |
| Vertices | $(h \pm a, k)$ | $(h, k \pm a)$ |
| Co-vertices | $(h, k \pm b)$ | $(h \pm b, k)$ |

3. Write an equation for the ellipse with vertices at $(6,-8)$ and $(6,4)$ and co-vertices at $(3,-2)$ and $(9,-2)$.
4. Write an equation for the ellipse with vertices at $(-3,8)$ and $(9,8)$ and co-vertices at $(3,12)$ and $(3,4)$.
5. Find the coordinates of the center and foci, and the lengths of the major and minor axes of an ellipse with equation $25 x^{2}+9 y^{2}+250 x-36 y+436=0$. Then graph the ellipse.

6. Find the coordinates of the center and foci and the lengths of the major and minor axes of the ellipse with equation $x^{2}+4 y^{2}-2 x+24 y+21=0$. Then graph the ellipse.

7. Find the coordinates of the center and foci and the lengths of the major and minor axes of the ellipse with equation $\frac{(y+1)^{2}}{64}+\frac{(x-5)^{2}}{28}=1$. Then graph the ellipse.

8. Find the coordinates of the center and foci and the lengths of the major and minor axes of the ellipse with equation $4 x^{2}+y^{2}-32 x-4 y+52=0$. Then graph the ellipse.

