## Big Idea \#4 Integral and Accumulation

| Concept | Question |
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| 1. Left Riemann Sum | Find the area under the curve $y=\sqrt{1-x^{2}}$ from 0 to 1 using a LRAM with 5 rectangles. |
| 2. Right Riemann Sum | Find the area under the curve $y=\sqrt{1-x^{2}}$ from 0 to 1 using a RRAM with 5 rectangles. |
| 3. Midpoint Riemann Sum | Find the area under the curve $y=\sqrt{1-x^{2}}$ from 0 to 1 using a MRAM with 4 rectangles. |
| 4. Trapezoidal Sum | $x$ -5 -3 0 1 5 <br> $f(x)$ 10 7 5 8 11 <br> Given the values for $f(x)$ on the table above, approximate the area under the graph of $f(x)$ from $x=-5$ to $x=5$ using four subintervals and a Trapezoidal approximation. |


| 5. Properties of Integrals | Given $\int_{0}^{5} f(x) d x=10$ and $\int_{5}^{7} f(x) d x=3$, find <br> a) $\int_{0}^{7} f(x) d x$ <br> b) $\int_{5}^{0} f(x) d x$ <br> c) $\int_{5}^{5} f(x) d x$ <br> d) $\int_{0}^{5} 3 f(x) d x$ |
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| 6. Calculating Integrals Using Geometry | Find the following: <br> a. $\int_{-2}^{0} \sqrt{4-x^{2}} d x$ <br> b. $\int_{-5}^{0}\|x+4\| d x$ |
| 7. Basic Antiderivative | $\int \frac{1}{3} x^{4} d x$ |
| 8. Trig Antiderivative | $\begin{array}{ll} \int \cos x d x & \int \sec x \tan x d x \\ \int \sin x d x & \int \csc ^{2} x d x \\ \int \sec ^{2} x d x & \int \csc x \cot x d x \end{array}$ |
| 9. Inverse Trig Antiderivative | $\int \frac{1}{x^{2}+1} d x \quad \int \frac{1}{\sqrt{1-x^{2}}} d x \quad \int \frac{1}{\|x\| \sqrt{x^{2}-1}} d x$ |
| 10. Fundamental Theorem of Calculus Part 1 | Find $\frac{d}{d x} \int_{2}^{x^{2}} \cos (t) d t$ |


| 11. Fundamental Theorem of Calculus Part 2 | Let $f$ be a function defined on the closed interval $-5 \leq x \leq 5$ with $f(1)=3$. The graph of $f^{\prime}$ the derivative of $f$, consists of two semicircles and two line segments, as shown below. Find the absolute minimum value of $f(x)$ over the closed interval $-5 \leq x \leq 5$. Explain your reasoning. |
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| 12. Average Mean Value | Find the average value of $f(x)=x^{2}+1$ from -1 to 3 . |
| 13. U-sub | $\int_{0}^{\pi} \cos \sqrt{\sin x} d x$ |
| 14. Slope Field | Shown above is the slope field for which of the following differential equations? <br> (A) $\frac{d y}{d x}=1+x$ <br> (B) $\frac{d y}{d x}=x^{2}$ <br> (C) $\frac{d y}{d x}=x+y$ <br> (D) $\frac{d y}{d x}=\frac{x}{y}$ <br> (E) $\frac{d y}{d x}=\ln y$ |



17. Area Between Curves $\quad$\begin{tabular}{l}
Let $R$ be the region in the first quadrant bounded by the $x$-axis and the graphs of $y=\ln x$ and $y=5-x$, as <br>
shown in the figure above. <br>
(a) Find the area of $R$. <br>
18. Volume $\rightarrow$ Cross Sections <br>

| Let $R$ be the region in the first quadrant bounded by the $x$-axis and the graphs of $y=\ln x$ |
| :--- |
| shown in the figure above. |
| (b) Region $R$ is the base of a solid. For the solid, each cross section perpendicular to the $x$-xis is a square |
| Write, but do not evaluate, an expression involving one or more integrals that gives the volume of the solid. | <br>

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\end{tabular}

19. Volume $\rightarrow$ Disks
