

No Calculator!

1) Write an explicit formula for the sequence $\frac{2}{4}, \frac{3}{7}, \frac{4}{12}, \frac{5}{19}, \frac{6}{42}, \dots$. Then find a_{14} .

A $a_n = a_{n-1} - \frac{n-1}{7n}; \frac{15}{199}$

C $a_n = \frac{n+1}{n^2+3}; \frac{15}{199}$

B $a_n = \frac{a_{n+1}}{n^2+3}; \frac{15}{199}$

D $a_n = \frac{n}{n^3-1}; \frac{14}{2743}$

2) Write the explicit formula for the sequence. Then find the fifth term in the sequence: $a_1 = 3, r = -3$.

A $a_n = 3 \cdot (-3)^{n-1}; 243$

C $a_n = 3 \cdot (3)^n; 243$

B $a_n = -3 \cdot (3)^{n-1}; -243$

D $a_n = 3 \cdot (-3)^n; -729$

3) Determine whether the sequence defined by

$$a_n = n^2 \cos\left(\frac{2}{n^2} + \frac{\pi}{2}\right)$$

converges or diverges. If it converges, find its limit.

a. -2

c. 0

b. -1

d. π

e. Diverges

4) The sequence $a_n = \sin \frac{n\pi}{6}$

- (A) is unbounded ~~(B) is monotonic~~
(C) converges to a number less than 1 (D) is bounded
(E) diverges to infinity

5) If $s_n = \left(\frac{(5+n)^{100}}{5^{n+1}} \right) \left(\frac{5^n}{(4+n)^{100}} \right)$, to what number does the sequence $\{s_n\}$ converge?

1993 BC
31 Calc

- (A) $\frac{1}{5}$ (B) 1 (C) $\frac{5}{4}$ (D) $\left(\frac{5}{4}\right)^{100}$ (E) The sequence does not converge.

6) If k is a positive integer, then $\lim_{x \rightarrow +\infty} \frac{x^k}{e^x}$ is

1988 BC 35

- (A) 0 (B) 1 (C) e (D) $k!$ (E) nonexistent

7) Show which function, $\ln x$ or $\log_2 x$ grows faster.

*will be one on the test and will NOT be multiple choice

8) $\lim_{x \rightarrow 0^+} \frac{\cot x}{\ln x} =$

- (A) $-\infty$ (B) -1 (C) 0 (D) 1 (E) ∞

9) $\lim_{x \rightarrow 0} \frac{1 - \cos^2(2x)}{x^2} =$

1973 BC 37

- (A) -2 (B) 0 (C) 1 (D) 2 (E) 4

10) $\lim_{x \rightarrow \frac{\pi}{4}} \frac{\sin\left(x - \frac{\pi}{4}\right)}{x - \frac{\pi}{4}}$ is

1985 BC 29

- (A) 0 (B) $\frac{1}{\sqrt{2}}$ (C) $\frac{\pi}{4}$ (D) 1 (E) nonexistent

11) $\lim_{x \rightarrow 0} \frac{\tan 3x}{2x} =$

- (A) 0 (B) $\frac{1}{2}$ (C) $\frac{2}{3}$ (D) $\frac{3}{2}$ (E) ∞

12) $\lim_{x \rightarrow 1} \frac{\int_1^x e^{t^2} dt}{x^2 - 1}$ is

1998 BC 28

- (A) 0 (B) 1 (C) $\frac{e}{2}$ (D) e (E) nonexistent

13) $\int_0^{\infty} xe^{x^2} dx$

a. 0

c. $\frac{1}{2}$

b. Divergent

b. $-\frac{1}{2}$

d. 1

14) $\int_2^{+\infty} \frac{dx}{x^2}$ is

1988 BC 7

(A) $\frac{1}{2}$

(B) $\ln 2$

(C) 1

(D) 2

(E) nonexistent

15) Which of the following improper integrals diverges?

(A) $\int_0^{\infty} e^{-x^2} dx$ (B) $\int_{-\infty}^0 e^x dx$ (C) $\int_0^1 \frac{dx}{x}$

(D) $\int_0^{\infty} e^{-x} dx$ (E) $\int_0^1 \frac{dx}{\sqrt{x}}$

16) $\int_{-\infty}^{\infty} \frac{2}{1+x^2} dx$

a. 0

c. $\frac{\pi}{2}$

b. 2π

b. π

c. Divergent