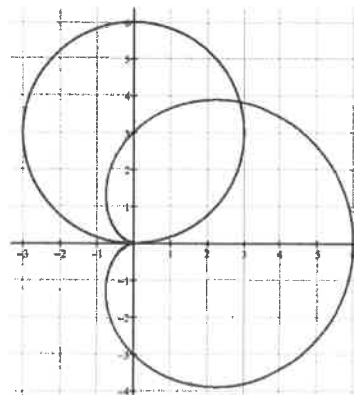


## Chapter 11 Review

Name: \_\_\_\_\_ Date: \_\_\_\_\_ Period: \_\_\_\_\_

1. The figure to the left shows the graph of  $r = 6 \sin \theta$  and  $r = 3 + 3 \cos \theta$  for  $0 \leq \theta \leq 2\pi$ .

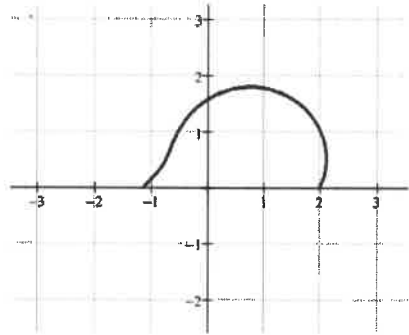
- a. Set up an equation to find the value of  $\theta$  for the intersection(s) of both graphs. Use your calculator to solve your equation and find the coordinates of the point(s) of intersection.



- b. Set up an expression with two or more integrals to find the area common to both curves. Evaluate the integrals.

2. The figure to the right shows the graph of  $r = \theta + 2 \cos \theta$  for  $0 \leq \theta \leq \pi$ .

- a. Find the area bounded by the curve and the x-axis



- b. Find an expression for  $\frac{dr}{d\theta}$ . Evaluate your expression for  $\frac{dr}{d\theta}$  at  $\theta = \frac{\pi}{3}$ . Write a sentence interpreting your result.

- c. Find the value of  $\theta$  for  $0 \leq \theta \leq \frac{\pi}{2}$  that corresponds to the point on the curve in the first quadrant with greatest distance to the origin. Justify your answer.

- d. Find the slope of the point where  $\theta = \frac{\pi}{3}$ . Show all of your work.

3. A particle moves in the  $xy$ -plane with position vector  $\langle x(t), y(t) \rangle$  such that  $x(t) = t^3 - 6t^2 + 9t + 1$  and  $y(t) = -t^2 + 6t + 2$  in the time interval  $0 \leq t \leq 5$ .
- Find the velocity vector of the particle at  $t = 5$ .
  - Is the particle moving to the left or to the right when  $t = 5$ ? Is the particle moving up or down when  $t = 5$ ? Justify your answer.
  - Find the equation of the tangent line to the path of the particle when  $t = 5$ .
  - At what time is the particle at rest? Justify your answer.
  - Find the acceleration vector at the time when the particle is at rest.
  - How fast is the particle moving when  $t = 5$ ?

- g. Find the total distance traveled by the particle for the time interval  $0 \leq t \leq 5$ .
- h. If the path followed by the particle was graphed, would the graph be concave up or down at  $t = 5$ ?
4. What are the points of tangency of the graph of the parametric equations  $x = t^2$  and  $y = \frac{t}{1+t}$ ?

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The length of the path described by the parametric equations  $x = \frac{1}{3}t^3$  and  $y = \frac{1}{2}t^2$ , where  $0 \leq t \leq 1$ , is given by

1998 BC 21

- (A)  $\int_0^1 \sqrt{t^2 + 1} dt$
- (B)  $\int_0^1 \sqrt{t^2 + t} dt$
- (C)  $\int_0^1 \sqrt{t^4 + t^2} dt$
- (D)  $\frac{1}{2} \int_0^1 \sqrt{4 + t^4} dt$
- (E)  $\frac{1}{6} \int_0^1 t^2 \sqrt{4t^2 + 9} dt$

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The length of the path described by the parametric equations  $x = \cos^3 t$  and  $y = \sin^3 t$ , for  $0 \leq t \leq \frac{\pi}{2}$ , is given by

1997 BC  
15

- (A)  $\int_0^{\frac{\pi}{2}} \sqrt{3 \cos^2 t + 3 \sin^2 t} dt$
- (B)  $\int_0^{\frac{\pi}{2}} \sqrt{-3 \cos^2 t \sin t + 3 \sin^2 t \cos t} dt$
- (C)  $\int_0^{\frac{\pi}{2}} \sqrt{9 \cos^4 t + 9 \sin^4 t} dt$
- (D)  $\int_0^{\frac{\pi}{2}} \sqrt{9 \cos^4 t \sin^2 t + 9 \sin^4 t \cos^2 t} dt$
- (E)  $\int_0^{\frac{\pi}{2}} \sqrt{\cos^6 t + \sin^6 t} dt$

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The area of the region enclosed by the polar curve  $r = 1 - \cos \theta$  is

1973 BC 40

- (A)  $\frac{3}{4}\pi$       (B)  $\pi$       (C)  $\frac{3}{2}\pi$       (D)  $2\pi$       (E)  $3\pi$

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The area of the closed region bounded by the polar graph of  $r = \sqrt{3 + \cos \theta}$  is given by the integral

1969 BC  
9

- (A)  $\int_0^{2\pi} \sqrt{3 + \cos \theta} d\theta$       (B)  $\int_0^{\pi} \sqrt{3 + \cos \theta} d\theta$       (C)  $2 \int_0^{\pi/2} (3 + \cos \theta) d\theta$   
(D)  $\int_0^{\pi} (3 + \cos \theta) d\theta$       (E)  $2 \int_0^{\pi/2} \sqrt{3 + \cos \theta} d\theta$